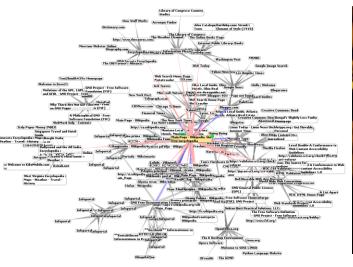
A Framework for Processing Large Graphs in Shared Memory

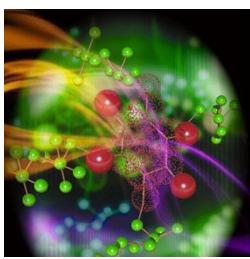
Julian Shun

What are graphs?









Graph Data is Everywhere!

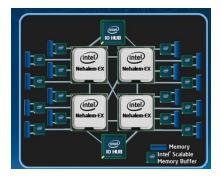
- Can contain up to billions of vertices and edges
- Need simple, efficient, and scalable ways to analyze them

Efficient Graph Processing

Use parallelism









Design efficient algorithms

Breadth-first search
Betweenness centrality
Connected components

Single-source shortest paths Eccentricity estimation (Personalized) PageRank

. . .

- Write/optimize code for each application
- Build a general framework

Ligra Graph Processing Framework

EdgeMap

VertexMap

Breadth-first search
Betweenness centrality
Connected components
Triangle counting
K-core decomposition
Maximal independent set
Set cover

Single-source shortest paths
Eccentricity estimation
(Personalized) PageRank
Local graph clustering
Biconnected components
Collaborative filtering

Simplicity, Performance, Scalability

Graph Processing Systems

 Existing: Pregel/Giraph/GPS, GraphLab, Pegasus, Knowledge Discovery Toolbox, GraphChi, etc.

 Our system: Ligra - Lightweight graph processing system for shared memory

Takes advantage of "frontier-based" nature of many algorithms (active set is dynamic and often small)

Breadth-first Search (BFS)

 Compute a BFS tree rooted at source r containing all vertices reachable from r

Applications

Betweenness centrality

Eccentricity estimation

Maximum flow

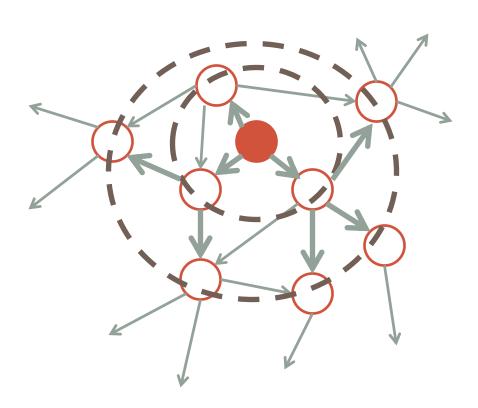
Web crawlers

Network broadcasting

Cycle detection

. . .





- Can process each frontier in parallel
- Race conditions, load balancing

Steps for Graph Traversal

Many graph traversal algorithms do this!

Operate on a subset of vertices

VertexSubset

- Map computation over subset of edges in parallel
- EdgeMap

Return new subset of vertices

VertexMap

Map computation over subset of vertices in parallel

We built the **Ligra** abstraction for these kinds of computations

Think with flat data-parallel operators

Abstraction enables optimizations (hybrid traversal and graph compression)

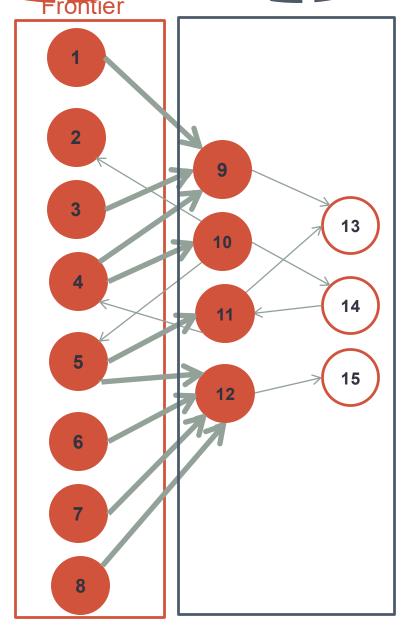
Breadth-first Search in Ligra

```
parents = {-1, ..., -1}; //-1 indicates "unexplored"
procedure UPDATE(s, d):
   return compare and swap(parents[d], -1, s);
procedure COND(v):
   return parents[v] == -1; //checks if "unexplored"
                                frontier
procedure BFS(G, r):
   parents[r] = r;
   frontier = {r}; //VertexSubset
                                frontier
   while (size(frontier) > 0):
           frontier = EDGEMAP(G, frontier, UPDATE, COND);
```

Actual BFS code in Ligra

```
#include "ligra.h"
struct BFS F {
 intT* Parents:
 BFS F(intT* Parents) : Parents( Parents) {}
 inline bool update (intT s, intT d) { //Update
   if(Parents[d] == -1) { Parents[d] = s; return 1; }
   else return 0:
 inline bool updateAtomic (intT s, intT d){ //atomic version of Update
   return (CAS(&Parents[d],(intT)-1,s));
 //cond function checks if vertex has been visited yet
 inline bool cond (intT d) { return (Parents[d] == -1); }
template <class vertex>
void Compute(graph<vertex> GA, intT start) {
 intT n = GA.n;
 //creates Parents array, initialized to all -1, except for start
 intT* Parents = newA(intT,GA.n);
 parallel_for(intT i=0;i<GA.n;i++) Parents[i] = -1;</pre>
 Parents[start] = start;
 vertexSubset Frontier(n,start); //creates initial frontier
 while(!Frontier.isEmpty()){ //loop until frontier is empty
   vertexSubset output = edgeMap(GA, Frontier, BFS F(Parents));
   Frontier.del():
   Frontier = output; //set new frontier
 Frontier.del():
 free(Parents):
```

Sparse or Dense EdgeMap?



- Dense method better when frontier is large and many vertices have been visited
- Sparse (traditional) method better for small frontiers
- Switch between the two methods based on frontier size [Beamer et al. SC '12]

Limited to BFS?

EdgeMap

```
procedure EDGEMAP(G, frontier, Update, Cond):

if (size(frontier) + sum of out-degrees > threshold) then:

return EDGEMAP_DENSE(G, frontier, Update, Cond);

else:

return EDGEMAP_SPARSE(G, frontier, Update, Cond);
```

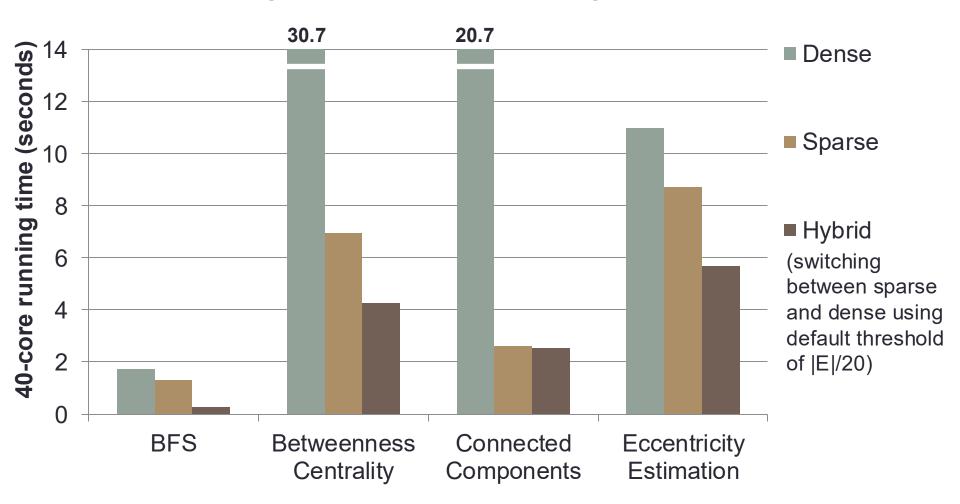
Loop through outgoing edges of frontier vertices in parallel

Loop through incoming edges of "unexplored" vertices (in parallel), breaking early if possible

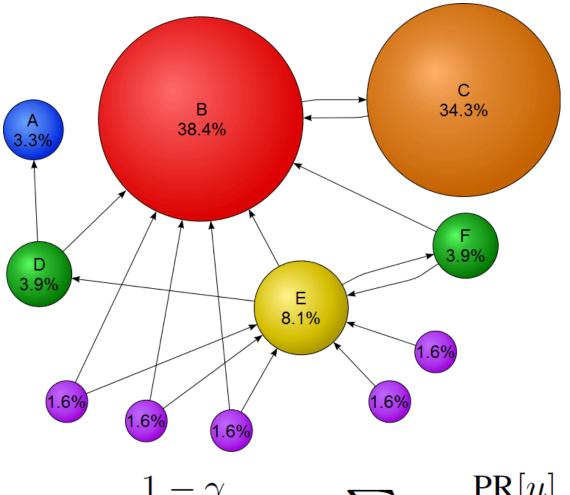
- More general than just BFS!
- Generalized to many other problems
 - For example, betweenness centrality, connected components, sparse PageRank, shortest paths, eccentricity estimation, graph clustering, k-core decomposition, set cover, etc.
- Users need not worry about this

Frontier-based approach enables hybrid traversal

Twitter graph (41M vertices, 1.5B edges)

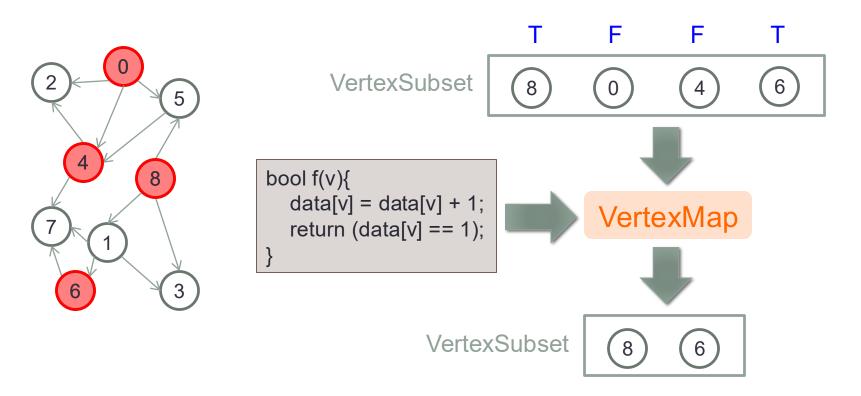


PageRank



$$\text{PR}[v] = \frac{1-\gamma}{|V|} + \gamma \sum_{u \in N^-(v)} \frac{\text{PR}[u]}{\text{deg}^+(u)}$$

VertexMap



PageRank in Ligra

```
p curr = \{1/|V|, ..., 1/|V|\}; p next = \{0, ..., 0\}; diff = \{\};
                                                                              error =∞;
procedure UPDATE(s, d):
     atomic increment(p next[d], p curr[s] / degree(s));
     return 1;
procedure COMPUTE(i):
     p next[i] = \alpha \cdot p_next[i] + (1-\alpha) \cdot (1/|V|);
     diff[i] = abs(p next[i] - p curr[i]);
     p curr[i] = 0;
     return 1;
procedure PageRank(G, \alpha, \epsilon):
    frontier = {0, ..., |V|-1};
     while (error > \varepsilon):
            frontier = EDGEMAP(G, frontier, UPDATE, COND<sub>true</sub>);
            frontier = VERTEXMAP(frontier, COMPUTE);
            error = sum of diff entries;
            swap(p curr, p next)
     return p curr;
```

PageRank

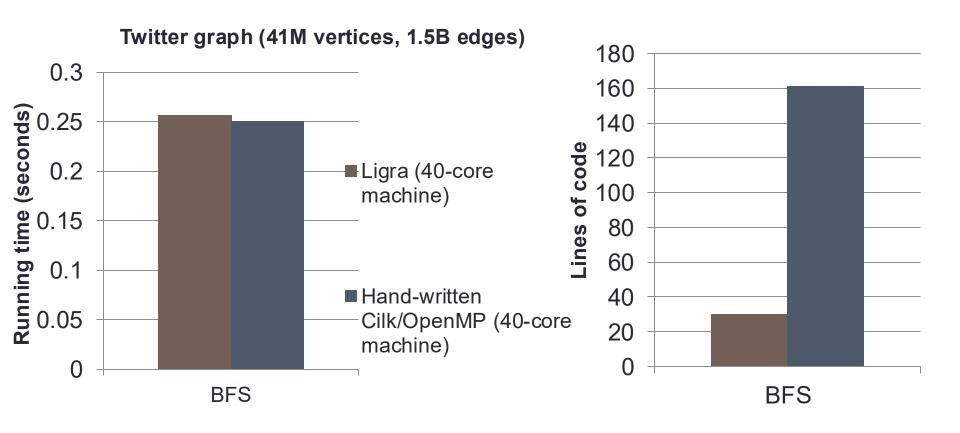
- Sparse version?
 - PageRank-Delta: Only update vertices whose PageRank value has changed by more than some Δ-fraction (discussed in PowerGraph and McSherry WWW '05)

PageRank-Delta in Ligra

```
PR[i] = \{1/|V|, ..., 1/|V|\};
nghSum = \{0, ..., 0\};
Change = {};
             //store changes in PageRank values
procedure UPDATE(s, d): //passed to EdgeMap
    atomic increment(nghSum[d], Change[s] / degree(s));
     return 1;
procedure COMPUTE(i): //passed to VertexMap
     Change[i] = \alpha \cdot \text{nghSum[i]};
     PR[i] = PR[i] + Change[i];
     return (abs(Change[i]) > \Delta); //check if absolute value of change is big enough
```

Performance of Ligra

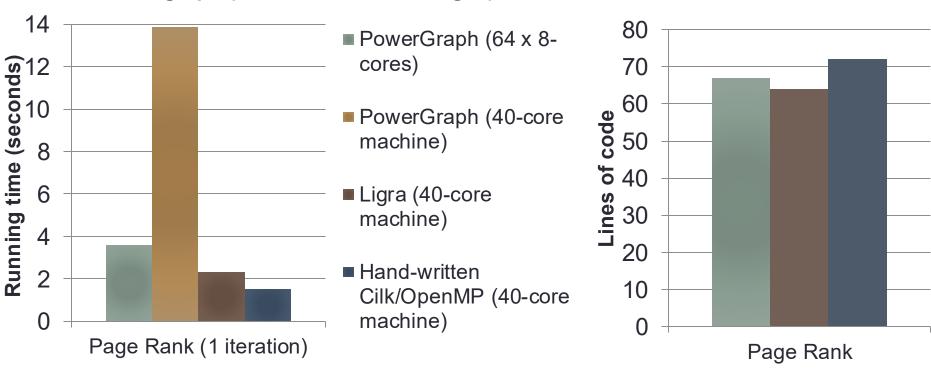
Ligra BFS Performance



Comparing against hybrid traversal BFS code by Beamer et al.

Ligra PageRank Performance

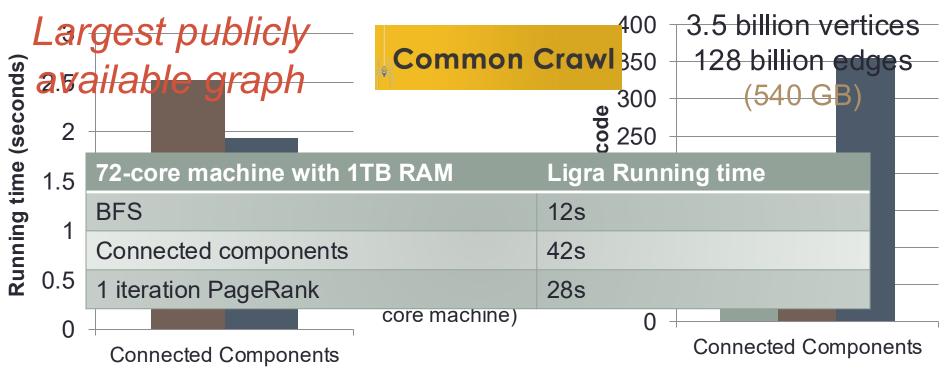
Twitter graph (41M vertices, 1.5B edges)



Easy to implement "sparse" version of PageRank in Ligra

Connected Components Performance

Twitter graph (41M vertices, 1.5B edges)



- Ligra's performance is close to hand-written code
- Faster than best existing system
- Subsequent systems have used Ligra's abstraction and hybrid traversal idea, e.g., Galois [SOSP '13], Polymer [PPoPP '15], Gunrock [PPoPP '16], Gemini [OSDI '16], GraphGrind [ICS '17], Grazelle [PPoPP '18]

Large Graphs

Amazon EC2

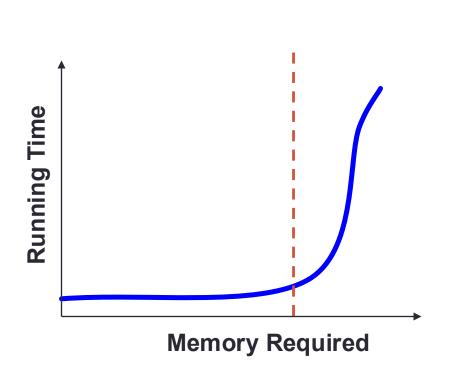
	vCPU	ECU	Memory (GiB)	Instance Storage (GB)	Linux/UNIX Usage
x1e.xlarge	4	12	122	1 x 120 SSD	\$0.834 per Hour
x1e.2xlarge	8	23	244	1 x 240 SSD	\$1.668 per Hour
x1e.4xlarge	16	47	488	1 x 480 SSD	\$3.336 per Hour
x1e.8xlarge	32	91	976	1 x 960	\$6.672 per Hour
x1e.16xlarge	64	179	1952	1 x 1920 SSD	\$13.344 per Hour
x1e.32xlarge	128	340	3904	2 x 1920 SSD	\$26.688 per Hour

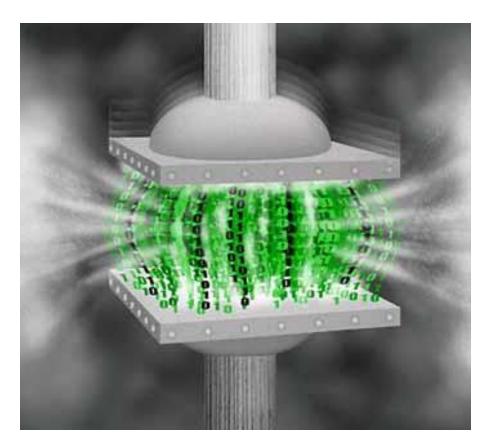
Most can fit on commodity shared memory machine



Example
Dell PowerEdge R930:
Up to 96 cores and 6 TB of RAM

What if you don't have or can't afford that much memory?

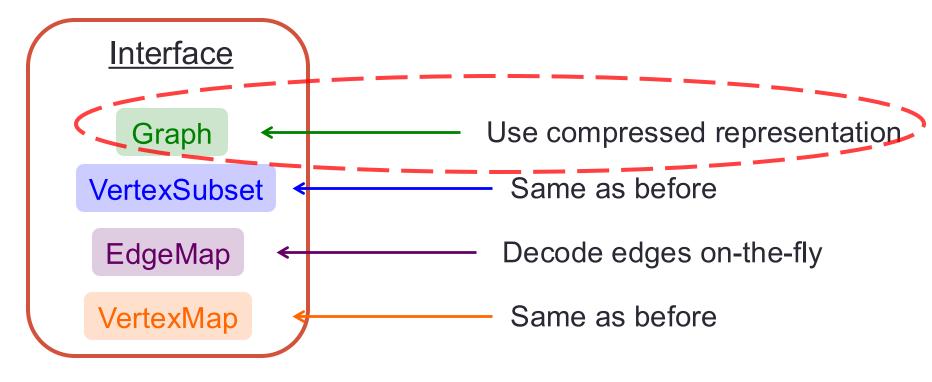




Graph Compression

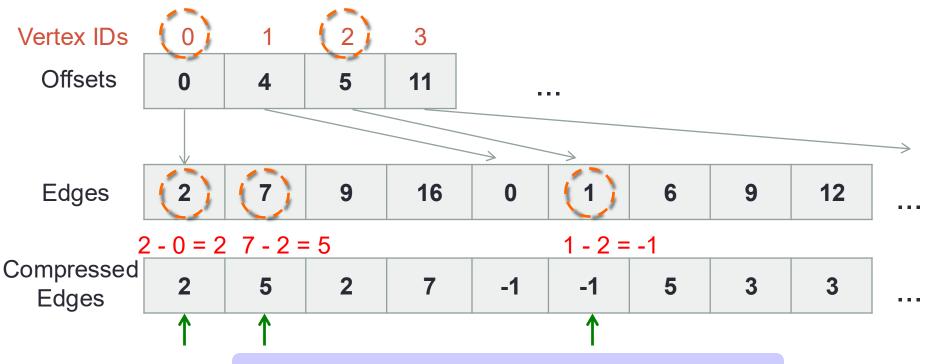
Ligra+: Adding Graph Compression to Ligra

Ligra+: Adding Graph Compression to Ligra



- Same interface as Ligra
- All changes hidden from the user!

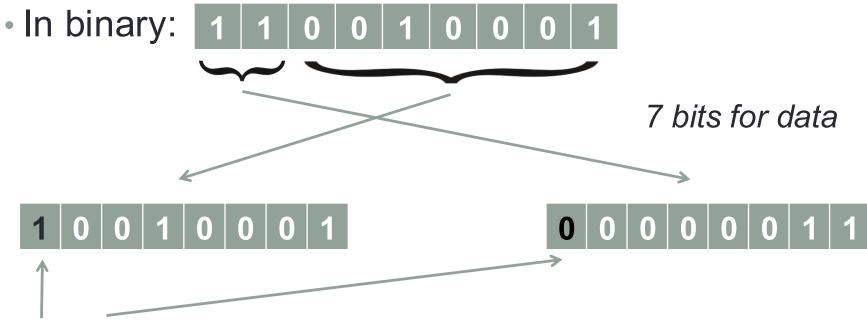
Graph representation



Sort edges and encode differences

Variable-length codes

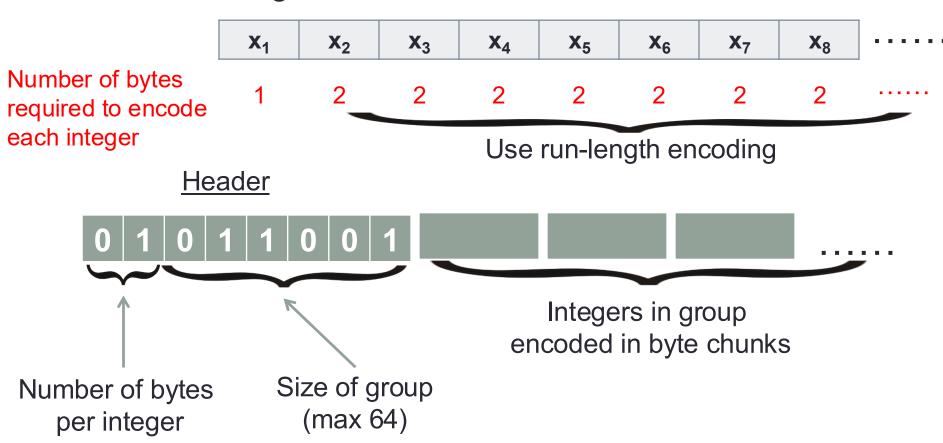
- k-bit codes
 - Encode value in chunks of k bits
 - Use k-1 bits for data, and 1 bit as the "continue" bit
- Example: encode "401" using 8-bit (byte) code



"continue" bit

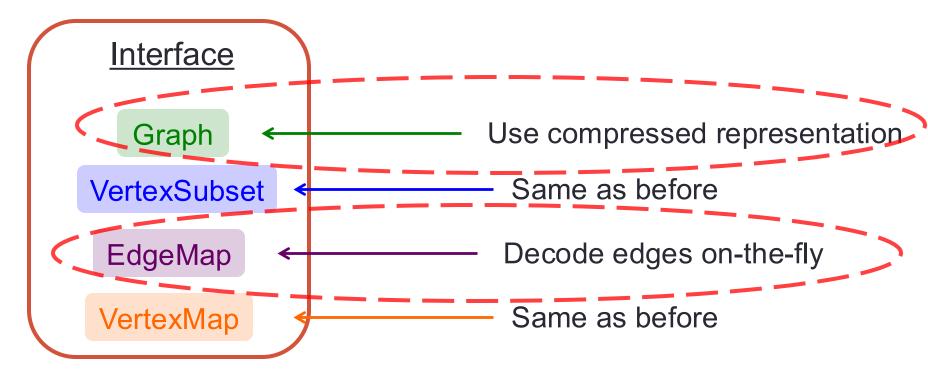
Encoding optimization

Another idea: get rid of "continue" bits



 Increases space, but makes decoding cheaper (no branch misprediction from checking "continue" bit)

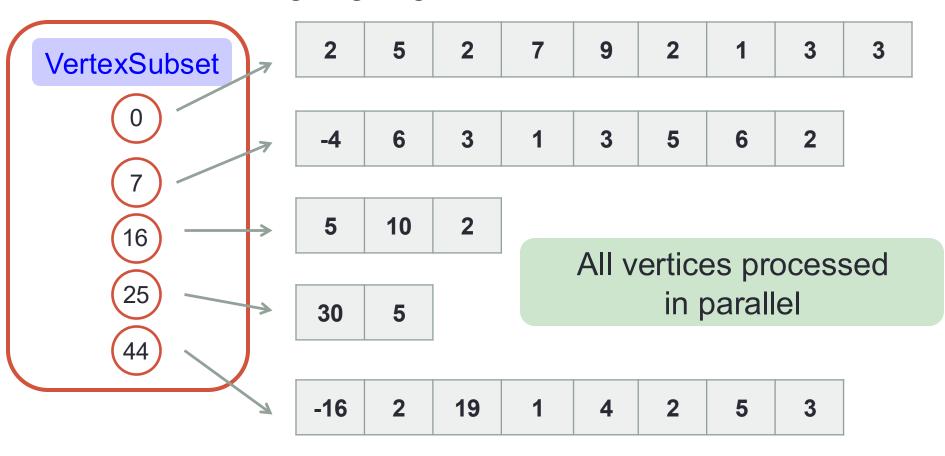
Ligra+: Adding Graph Compression to Ligra



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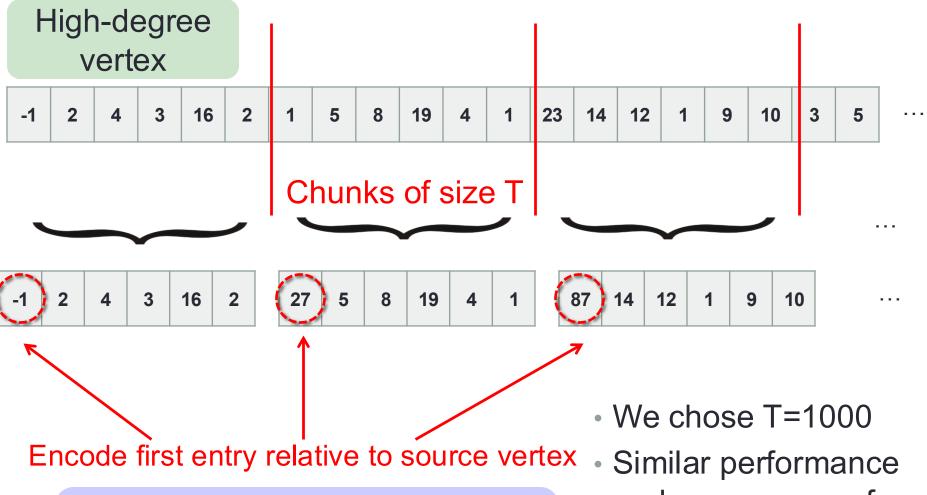
Modifying EdgeMap

Processes outgoing edges of a subset of vertices



What about high-degree vertices?

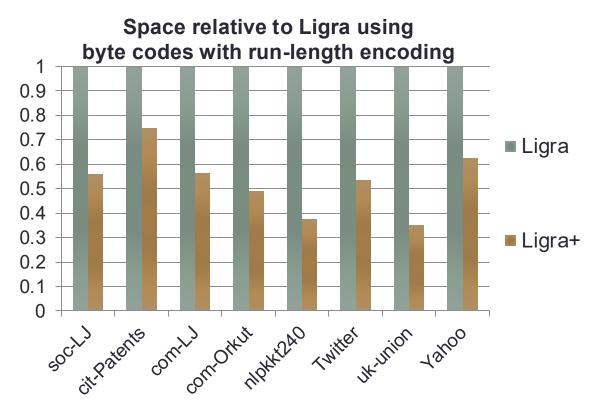
Handling high-degree vertices



All chunks can be decoded in parallel!

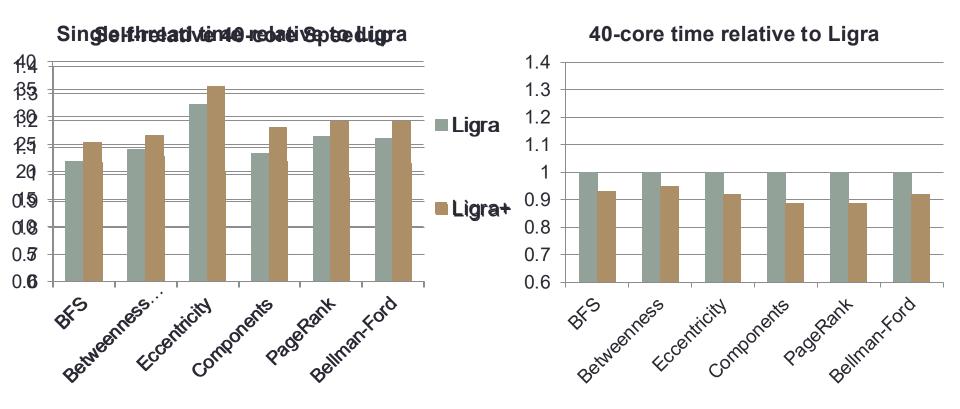
Similar performance and space usage for a wide range of T

Ligra+ Space Savings



- Space savings of about 1.3—3x
- Could use more sophisticated schemes to further reduce space, but more expensive to decode
- Cost of decoding on-the-fly?

Ligra+ Performance



- Cost of decoding on-the-fly?
- Memory subsystem is a scalability bottleneck in parallel as these graph algorithms are memory-bound
- Ligra+ decoding gets better parallel speed up

Ligra Summary

VertexSubset

VertexMap

EdgeMap

Optimizations: Hybrid traversal and graph compression

Breadth-first search
Betweenness centrality
Connected components
Triangle counting
K-core decomposition
Maximal independent set

Single-source shortest paths
Eccentricity estimation
(Personalized) PageRank
Local graph clustering
Biconnected components
Collaborative filtering

. . .

Simplicity, Performance, Scalability



- J. Shun and G. E. Blelloch. Ligra: *A Lightweight Graph Processing Framework for Shared Memory*, Principles and Practice of Parallel Programming, 2013.
- J. Shun, L. Dhulipala and G. E. Blelloch. Smaller and Faster: *Parallel Processing of Compressed Graphs with Ligra+*, Data Compression Conference, 2015.

Code: https://github.com/jshun/ligra/